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Roll No. :

328651(28)

B. E. (Sixth Semester) Examination April-May 2021

(New Scheme)

(Et & T Engg. Br.)

DIGITAL SIGNAL PROCESSING

Time Allowed : Three hours

Maximum Marks : 80

Minimum Pass Marks : 28

Note : Attempt all questions. Part (a) of each question is compulsory. Attempt any two parts from (b), (c) and (d) of each question.

Unit - I

1. (a) Define convolution. 2
- (b) Compute circular periodic convolution of the two

[2]

sequences $x_1(n) = \{1, 1, 2, 2\}$ and

$x_2(n) = \{1, 2, 3, 4\}$. 7

(c) Given $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$, find $X(k)$ using DITFFT algorithm. 7

(d) Given : 7

$$X(k) = \{36, -4 + j9 \cdot 656, -4 + j4, -4 - j1 \cdot 656, -4, -4 - j1 \cdot 656, -4j4, -4 - j9 \cdot 656\}$$

find $x(n)$.

Unit-II

2. (a) Define canonic and Non-canonic structures. 2

(b) Determine the direct form I realisation for a third order IIR transfer function. 7

$$H(z) = \frac{0.28z^2 + 0.319z + 0.04}{0.5z^3 + 0.3z^2 + 0.17z - 0.2}$$

(c) Obtain a cascade realisation of the system characterised by the transfer function

[3]

$$H(z) = \frac{2(z+2)}{z(z-0.1)(z+0.5)(z+0.4)} \quad 7$$

(d) Determine the parallel realisation of the IIR digital filter transfer functions.

$$H(z) = \frac{3(2z^2 + 5z + 4)}{(2z+1)(z+2)} \quad 7$$

Unit-III

3. (a) List advantages of FIR filter over IIR filter. 2

(b) A low-pass filter is to be designed with the following desired frequency response. 7

$$H_d(e^{jw}) = \begin{cases} e^{-j2w}, & -\pi/4 \leq w \leq \pi/4 \\ 0, & \pi/4 < |w| \leq \pi \end{cases}$$

Determine the filter coefficients $h_d(n)$, if the window function is defined as

$$w(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

determine filter coefficients of the designed filter $h(n)$.

[4]

- (c) The desired response of a low pass filter is :

$$H_d(e^{jw}) = \begin{cases} e^{-j3w}, & -3\pi/4 \leq w \leq 3\pi/4 \\ 0, & 3\pi/4 < |w| \leq \pi \end{cases}$$

Determine $H(e^{jw})$ for $M = 7$ using a Hamming window.

- (d) Describe the filter design procedure using Kaiser window function.

Unit-IV

4. (a) Define frequency warping.
 (b) Convert the analog filter into a digital filter whose system function is :

$$H(s) = \frac{s + 0.2}{(s + 0.2)^2 + 9}$$

Use the impulse invariant technique.

Assume $T = 1s$.

- (c) Design a digital Butterworth filter that satisfies the following constraint using bilinear transformation.

[5]

Assume $T = 1s$

$$0.9 \leq |H(e^{jw})| \leq 1 \quad 0 \leq w \leq \pi/2$$

$$|H(e^{jw})| \leq 0.2 \quad 3\pi/4 \leq w \leq \pi$$

- (d) Design a digital Chebyshev filter to satisfy the constraints

$$0.707 \leq |H(e^{jw})| \leq 1 \quad 0 \leq w \leq 0.2\pi$$

$$|H(e^{jw})| \leq 0.1 \quad 0.5\pi \leq w \leq \pi$$

Using bilinear transformation and assuming $T = 1s$

Unit - V

5. (a) Define upsampler and downsampler.
 (b) Obtain the expression for the output $y(n)$ in terms of $x(n)$ for the multirate systems given as follows :
 $x(n) \rightarrow \boxed{\uparrow 5} \rightarrow \boxed{\downarrow 20} \rightarrow \boxed{\uparrow 4} \rightarrow y(n)$
 (c) Obtain the polyphase decomposition of the IIR system with transfer function :

[6]

$$H(z) = \frac{1 - 4z^{-1}}{1 + 5z^{-1}} \quad 7$$

- (d) Obtain the two-fold expanded signal $y(n]$ of the input signal $x(n]$.

$$x(n] = \begin{cases} n, & n > 0 \\ 0, & \text{otherwise} \end{cases} \quad 7$$